

Name: .....

1] Please complete the following sentences:

A] A subset  $H$  of a group  $G$  is a *subgroup* if and only if the following two conditions hold:

- for every  $h, k \in H$  .....
- for every  $h \in H$  .....

B] A subgroup  $H$  of a group  $G$  is *cyclic* if and only there exists .....

such that .....

C] A subgroup  $H$  of a group  $G$  is *normal* if and only if for every  $a \in G$  and for every  $h \in H$  .....

.....

2] Are the following statements true or false? Please circle your answers.

A] If  $H$  is a subgroup of a group  $G$  and  $G$  is abelian, then  $H$  is necessarily abelian.... TRUE | FALSE

B] If  $H$  is a subgroup of a group  $G$  and  $G$  is abelian, then  $H$  is necessarily normal.... TRUE | FALSE

C] If  $H$  is a subgroup of a group  $G$  and  $H$  is abelian, then  $H$  is necessarily normal... TRUE | FALSE

D] If  $H$  is a subgroup of a group  $G$  and  $G$  is cyclic, then  $H$  is necessarily cyclic..... TRUE | FALSE