Name: $\qquad$
For each of the following six questions, four possible answers are provided, but only one of them is correct: write the corresponding letter in the box!

1] Let $f: X \rightarrow Y$ be a function. Let $x$ and $x^{\prime}$ be elements of $X$ such that $x=x^{\prime}$.
What do we need to know about $f$ to conclude that $f(x)=f\left(x^{\prime}\right)$ ? $\qquad$
A] Nothing: this is true for all functions $f$.
B] We need $f$ to be injective.
C] We need $f$ to be surjective.
D] We need $f$ to be bijective.
2] Let $f: X \rightarrow Y$ be a function. Let $x$ and $x^{\prime}$ be elements of $X$ such that $f(x)=f\left(x^{\prime}\right)$.
What do we need to know about $f$ to conclude that $x=x^{\prime}$ ? $\qquad$
A] Nothing: this is true for all functions $f$.
B] We need $f$ to be injective.
C] We need $f$ to be surjective.
D] We need $f$ to be bijective.
3] Let $f: X \rightarrow Y$ be a function. Let $x$ and $x^{\prime}$ be elements of $X$ such that $f(x) \neq f\left(x^{\prime}\right)$.
What do we need to know about $f$ to conclude that $x \neq x^{\prime}$ ? $\square$
A] Nothing: this is true for all functions $f$.
B] We need $f$ to be injective.
C] We need $f$ to be surjective.
D] We need $f$ to be bijective.
4] Let $f: X \rightarrow Y$ be a function. Let $y$ be an element of $Y$.
What do we need to know about $f$ to conclude that $y=f(x)$ for some $x \in X$ ? $\qquad$
A] Nothing: this is true for all functions $f$.
B] We need $f$ to be injective.
C] We need $f$ to be surjective.
D] We need $f$ to be bijective.
5] Let $f: X \rightarrow Y$ be a function. Let $y$ be an element of $Y$.
What do we need to know about $f$ to conclude that $y=f(x)$ for exactly one $x \in X$ ? $\square$
A] Nothing: this is true for all functions $f$.
B] We need $f$ to be injective.
C] We need $f$ to be surjective.
D] We need $f$ to be bijective.
6] Let $f: X \rightarrow Y$ be a function. Let $x$ be an element of $X$.
What do we need to know about $f$ to conclude that $f(x)=y$ for exactly one $y \in Y$ ? $\square$
A] Nothing: this is true for all functions $f$.
B] We need $f$ to be injective.
C] We need $f$ to be surjective.
D] We need $f$ to be bijective.

